Astrophysical Radiation Mechanisms and Polarization



Markus Böttcher North-West University Potchefstroom, South Africa



- 1. Introduction to Radiation Transfer
- 2. Blackbody Spectrum Brightness Temperature
- 3. Introduction to Synchrotron Radiation (spectra, energy losses, polarization, Stokes parameters)
- Introduction to Compton Scattering (spectra, energy losses, Compton polarization, X-ray/γ-ray polarimetry)

Radiation Transfer





Radiation Transfer (II)



400 500 600 Wavelength (nm)

700

Radiation Transfer (III)

Special Cases

 $I_{v}(\tau_{v}) = I_{v}(0) e^{-\tau_{v}} + S_{v}(1 - e^{-\tau_{v}})$

2) Emission spectra

No significant background source

 $(\mathsf{I}_{v}(0) \approx \mathsf{0})$

I) Optically thick emission:

 $(\tau_v >> 1)$



Radiation Transfer (IV)

Special Cases

 $I_v(\tau_v) \approx I_v(0) e^{-\tau_v} + S_v(\eta \approx e_v^{\tau_v})$ s

2) Emission spectra

No significant background source

 $(\mathbf{I}_{\lambda}(0) \approx \mathbf{0})$

II) Optically thin emission:

 $(\tau_{\lambda} << 1)$





- 1. Introduction to Radiation Transfer
- 2. Blackbody Spectrum Brightness Temperature
- 3. Introduction to Synchrotron Radiation (spectra, energy losses, polarization, Stokes parameters)
- Introduction to Compton Scattering (spectra, energy losses, Compton polarization, X-ray/γ-ray polarimetry)

Thermal Blackbody Radiation

$$I_{v}(\tau_{v}) = I_{v}(0) e^{-\tau_{v}} + S_{v}(1 - e^{-\tau_{v}})$$



Thermal Blackbody Spectrum



Brightness Temperature

Define **Brightness Temperature** T_b by setting measured intensity I_v equal to Blackbody in Rayleigh-Jeans Limit:

$$I_v = 2 (v^2/c^2) k_B T_b$$

$$\Rightarrow \mathsf{T}_{\mathsf{b}} = \frac{I_{\nu} c^2}{2 \nu^2 k_B}$$

Note: T_b usually has nothing to do with the source's real temperature!

Brightness Temperature

Brightness temperatures $T_b > 10^{12}$ K seem unphysical because of strong Compton scattering (see point 4 below)



Relativistic Beaming / Boosting



Relativistic Beaming / Boosting



(if the size of the emitter is determined from variability)



- 1. Introduction to Radiation Transfer
- 2. Blackbody Spectrum Brightness Temperature
- 3. Introduction to Synchrotron Radiation (spectra, energy losses, polarization, Stokes parameters)
- Introduction to Compton Scattering (spectra, energy losses, Compton polarization, X-ray/γ-ray polarimetry)

Cyclotron/Synchrotron Radiation



Synchrotron Radiation

Relativistic electrons:

$$v_{sy}(\gamma) \sim 4.2^{*}10^{6}(B/G) \gamma^{2} Hz$$

Power output into synchrotron radiation (single electron):

$$\left(\frac{dE}{dt}\right)_{sy}(\gamma) = \frac{4}{3} c \sigma_{T} u_{B} \gamma^{2} \beta^{2}$$





Simple delta-function approximation for single-electron emissivity:

$$\mathsf{P}_{v}(\gamma) \approx \left(\frac{dE}{dt}\right)_{sy} \delta(v - v_{sy}[\gamma])$$

$$v_{sy}(\gamma) = v_0 \gamma^2$$

 $\begin{aligned} \mathbf{j}_{\mathbf{v}} &= \int_{1}^{\infty} d\gamma \; \mathsf{P}_{\mathbf{v}}(\gamma) \; \mathsf{N}_{\mathsf{e}}(\gamma) \sim \mathsf{N}_{\mathsf{e}}(\gamma_{\mathsf{c}}) \; \mathbf{v}^{1/2} \\ \\ &\gamma_{\mathsf{c}} = (\mathbf{v}/\mathbf{v}_{0})^{1/2} \end{aligned}$

Synchrotron Radiation

Power-law distribution of relativistic electrons:

 $N_e(\gamma) \sim \gamma^{-p}$

If there are electrons with $v = v_{sv} (\gamma)$, then:





Preferred direction of E-field vectors of radiation



 \overline{E}_{rad} predominantly \perp to projection of \overline{B}

Synchrotron Polarization

Calculate polarization-dependent intensities I_v^\perp and I_v^\parallel perpendicular and parallel to B-field projection

Degree of Polarization:
$$\Pi = \frac{I_{max} - I_{min}}{I_{max} + I_{min}} = \frac{I_v^{\perp} - I_v^{\parallel}}{I_v^{\perp} + I_v^{\parallel}}$$

In perfectly ordered, homogeneous B-field:

$$\Pi = \frac{p+1}{p+7/3} = \frac{\alpha+1}{\alpha+5/3} \qquad (\alpha = \frac{p-1}{2})$$

 $p = 2 \rightarrow \Pi = 69 \%$ $p = 3 \rightarrow \Pi = 75 \%$

Stokes Parameters



tan(2χ

Define Stokes Parameters:

 $\begin{array}{ll} I &= \mbox{Total intensity} & -> & \mbox{Polarized Intensity} \ I_{pol} = \Pi \ I \\ Q &= I_{pol} \ cos(2\beta) \ cos(2\chi) & (\beta = \mbox{phase-shift y vs. } x => \mbox{circ. pol.}) \\ U &= I_{pol} \ cos(2\beta) \ sin(2\chi) \\ V &= I_{pol} \ sin(2\beta) = \mbox{circularly polarized intensity (typically, } \beta << 1) \end{array}$



Stokes Parameters

Stokes parameters are additive:



Simply add up Stokes parameters from different zones:

 $I_{\text{total}} = \sum_{k=1}^{N} I_{k}$ $\Pi = \frac{\sqrt{Q_{\text{total}}^{2} + U_{\text{total}}^{2} + V_{\text{total}}^{2}}}{I_{\text{total}}}$ $U_{\text{total}} = \sum_{k=1}^{N} U_{k}$ $\tan(2\chi) = \frac{U_{\text{total}}}{Q_{\text{total}}}$ $V_{\text{total}} = \sum_{k=1}^{N} V_{k}$



- 1. Introduction to Radiation Transfer
- 2. Blackbody Spectrum Brightness Temperature
- 3. Introduction to Synchrotron Radiation (spectra, energy losses, polarization, Stokes parameters)
- Introduction to Compton Scattering (spectra, energy losses, Compton polarization, X-ray/γ-ray polarimetry)

Compton Scattering



For $\varepsilon' << 1 \rightarrow \varepsilon'_{s} \approx \varepsilon'$ (elastic scattering – Thomson Regime) For $\varepsilon' >> 1 \rightarrow \varepsilon'_{s} \sim 1$ (inelastic scattering – Klein-Nishina [KN] Regime)

$$\sigma_C(\epsilon') = \frac{\pi r_e^2}{\epsilon'^2} \left(4 + \frac{2\epsilon'^2 (1+\epsilon')}{(1+2\epsilon')^2} + \frac{\epsilon'^2 - 2\epsilon' - 2}{\epsilon'} \ln(1+2\epsilon') \right)$$

Compton Scattering



<u>Compton Scattering by Relativistic</u> <u>Electrons – Thomson Regime</u>



ph in electron rest frame ('): $\epsilon' = \epsilon \gamma (1 - \beta \mu)$ In Thomson Regime ($\epsilon' << 1$): $\epsilon_s' = \epsilon'$ Doppler boost into lab frame: $\epsilon_s = \gamma \epsilon_s' = \epsilon \gamma^2 (1 - \beta \mu)$

Concentrated in forward direction (Ω_e)

 $\frac{\text{Thomson approximation for differential cross section:}}{\frac{d\sigma_{C}}{d\epsilon \ d\Omega_{s}}} = \sigma_{T} \ \delta(\epsilon_{s} - \epsilon \ \gamma^{2} \left[1 - \beta \mu\right]) \ \delta(\Omega_{s} - \ \Omega_{e})$

Compton Losses and Spectra

Power output into Compton radiation (single electron):

$$\left(\frac{dE}{dt}\right)_{C}(\gamma) = \frac{4}{3} c \sigma_{T} u_{rad} \gamma^{2} \beta^{2}$$

Delta-function approximation for single-electron emissivity:

$$\begin{split} \mathsf{P}_{\nu}(\gamma) &\approx (\frac{dE}{dt})_{\mathsf{C}} \,\delta(\nu - \nu_{\mathsf{C}}[\gamma]) \\ \nu_{\mathsf{C}}(\gamma) &\sim \nu_{0} \,\gamma^{2} \\ \mathsf{j}_{\nu} &= \int_{1}^{\infty} d\gamma \, \mathsf{P}_{\nu}(\gamma) \,\mathsf{N}_{\mathsf{e}}(\gamma) \sim \mathsf{N}_{\mathsf{e}}(\gamma_{\mathsf{c}}) \,\nu^{1/2} \\ \gamma_{\mathsf{c}} &= (\nu/\nu_{0})^{1/2} \end{split}$$

Compton Spectra

Power-law distribution of relativistic electrons:

 $N_{e}(\gamma) \sim \gamma^{-p}$

If there are electrons with $v = v_{\rm C} (\gamma)$, then:



<u>Compton Scattering by Relativistic</u> <u>Electrons – KN Regime</u>

ph in electron rest frame ('): $\epsilon' = \epsilon \gamma (1 - \beta \mu)$ In the KN-Regime ($\epsilon' >> 1$): $\epsilon_s' = 1$ Doppler boost into lab frame: $\epsilon_s = \gamma \epsilon_s' = \gamma$

⇒ Photon takes all of the electron's energy ($\varepsilon_s \sim \varepsilon \gamma^2 > \gamma \rightarrow$ would violate energy conservation!)



Cut-off in the resulting Comptonscattered spectra around $\varepsilon_s \sim 1/\epsilon$



Compton Polarization

Compton cross section is polarization-dependent:

$$\frac{d\sigma}{d\Omega} = \frac{r_0^2}{4} \left(\frac{\epsilon'}{\epsilon}\right)^2 \left(\frac{\epsilon}{\epsilon'} + \frac{\epsilon'}{\epsilon} - 2 + 4\left[\overrightarrow{e} \cdot \overrightarrow{e'}\right]^2\right)$$

(e⁻ rest frame) $\epsilon = h\nu/(m_ec^2)$

Thomson regime: $\varepsilon \approx \varepsilon'$ $\Rightarrow d\sigma/d\Omega = 0$ if $\vec{e} \cdot \vec{e}' = 0$

 \Rightarrow Scattering preferentially in the plane perpendicular to $\vec{e!}$

Preferred EVPA is preserved.

Scattering of polarized rad. by relativistic $e^- => \Pi$ reduced to $\sim \frac{1}{2}$ of target-photon polarization.



X-ray Polarimeters



INTEGRAL





Scintillator CZT (5 & 2 mm thick) I6 cm I6 cm IG CM I

X-Calibur \rightarrow PolSTAR



XIPE

ASTROSAT

X-Ray Polarimeters







(POLAR: Kole et al. 2016)



Gamma-Ray Polarimetry with Fermi-LAT



e



e⁺e⁻ pair is preferentially produced in the plane of (\vec{k}, \vec{e}) of the γ -ray. Potentially detectable at E < 200 MeV \rightarrow PANGU / eASTROGAM





1. Introduction to Radiation Transfer

 Radiation Mechanisms: Introduction to Synchrotron Radiation (spectra, energy losses, polarization, Stokes parameters)

3. Introduction to Compton Scattering (spectra, energy losses, Compton polarization, X-ray/γ-ray polarimetry).

Introduction to γγ absorption / pair production, Doppler factor estimate from γγ opacity

<u>yy Absorption and Pair Production</u>

Threshold energy ε_{thr} of a γ -ray to interact with a background photon with energy ε_1 : 2





Delta-Function Approximation:

$$\sigma_{\gamma\gamma}^{\delta}(\epsilon_1,\epsilon_2) = \frac{1}{3} \,\sigma_T \,\epsilon_1 \,\delta\left(\epsilon_1 - \frac{2}{\epsilon_2}\right)$$

VHE gamma-rays interact preferentially with IR photons:

$$\lambda_2 = 2.4 E_{1,\text{TeV}} \ \mu\text{m}$$

<u>Spectrum of the Extrgalactic</u> <u>Background Light (EBL)</u>



EBL Absorption



<u>yy Absorption Intrinsic to the Source</u>

Optical depth to yy-absorption:

$$\tau_{\gamma\gamma}(\epsilon_{\gamma}) \sim n_{ph} \left(\frac{2}{\varepsilon_{\gamma}}\right) R \sigma_{T}$$

$$n_{ph} \sim \frac{L}{4\pi R^2 c \varepsilon m_e c^2} = \frac{4\pi d_L^2 F}{4\pi R^2 c \varepsilon m_e c^2}$$

Importance of intrinsic $\gamma\gamma$ -absorption is estimated by the <u>Compactness Parameter:</u>

$$\ell = \frac{L_{\gamma} \, \sigma_T}{4 \, \pi \, R \, \langle \epsilon \rangle \, m_e c^3}$$

<u>yy Absorption Intrinsic to the Source</u>

Estimate R from variability time scale:

 $R \sim c\Delta t_{var}$

Optical depth to yy-absorption:





With F_x and Δt_{var} from PKS 2155-304: $\tau_{\gamma\gamma}$ (ϵ_{TeV}) >> 1

Relativistic Beaming / Boosting



Relativistic Beaming / Boosting



<u>yy Absorption Intrinsic to the Source</u>

Optical depth to $\gamma\gamma$ -absorption:

$$\tau_{\gamma\gamma}(\epsilon_{\gamma}) \sim \frac{d_L^2 F_{\epsilon}(\frac{2}{\epsilon_{\gamma}})\sigma_T}{\Delta t_{var}(\frac{2}{\epsilon_{\gamma}})m_e c^4}$$

$$F_{\varepsilon} = \delta^{-(3+\alpha)} F_{\epsilon}^{obs}$$
$$\varepsilon_{\gamma} = \varepsilon_{\gamma}^{obs} / \delta$$
$$\Delta t_{var} = \delta \Delta t_{var}^{obs}$$

$$\Rightarrow au_{\gamma\gamma} \propto \delta^{-(5+lpha)}$$







- Class of AGN consisting of BL Lac objects and gamma-ray bright quasars
- Rapidly (often intra-day) variable
- Strong gamma-ray sources
- Radio jets, often with superluminal motion
- Radio and optical polarization

Blazar Spectral Energy Distributions (SEDs)



Flux and Polarization Variability

Multi-wavelength variability on various time scales (months – minutes) Sometimes correlated, sometimes not

Observed polarization fractions Π_{obs} <~ 10 % << Π_{max}

=> Not perfectly ordered magnetic fields!

Both degree of polarization and polarization angles vary. Swings in polarization angle sometimes associated with high-energy flares!



Open Physics Questions

- Source of Jet Power (Blandford-Znajek / Blandford/Payne?)
- Physics of jet launching / collimation / acceleration – role / topology of magnetic fields
- Composition of jets (e⁻-p or e⁺-e⁻ plasma?) leptonic or hadronic high-energy emission?
- Mode of particle acceleration (shocks / shear layers / magnetic reconnection?) - role of magnetic fields
- Location of the energy dissipation / gamma-ray emission region

<u>Blazar Models</u>



<u>Blazar Models</u>

Proton-

Injection, induced acceleration of radiation ultrarelativistic Relativistic jet outflow with $\Gamma \approx 10$ electrons and protons Narrow Line L > Region $Q_{e,p}$ (γ, t) ∿-d Broad Line ν Region • Proton Jet synchrotron • $p\gamma \rightarrow p\pi^0$ Black Accretion $\pi^0 \rightarrow 2\gamma$ Hole Disk • $p\gamma \rightarrow n\pi^+$; $\pi^+ \rightarrow \mu^+ \nu_{\mu}$ emission of $\mu^+ \rightarrow e^+ \nu_e \nu_\mu$ primary e Obscuring Torus \rightarrow secondary μ -, **L** > Hadronic e-synchrotron **Models** • Cascades ... ν

Requirements for lepto-hadronic models

- To exceed p- γ pion production threshold on interactions with synchrotron (optical) photons: $E_p > 7x10^{16} E^{-1}_{ph,eV} eV$
- For proton synchrotron emission at multi-GeV energies:
 E_p up to ~ 10¹⁹ eV (=> UHECR)
- Require Larmor radius

 $r_L \sim 3x10^{16} E_{19}/B_G cm ≤ a few x 10^{15} cm => B ≥ 10 G$ (Also: to suppress leptonic SSC component below synchrotron) – inconsistent with radio-core-shift measurements if emission region is located at ~ pc scales (e.g., Zdziarski & Böttcher 2015).

• Low radiative efficiency: Requiring jet powers $L_{jet} \sim L_{Edd}$

SED Model Fit Degeneracy

RGB J0710+591 (HBL)



Polarization Induced by Anisotropic Compton Scattering



 Thermal + Non-Thermal Electron Distributions from Diffusive Shock Acceleration

AO 0235+164



Expected Polarization from Bulk Compton



Polarization Induced by Anisotropic Scattering





Calculation of X-Ray and Gamma-Ray Polarization in Leptonic and Hadronic Blazar Models

Upper limits on high-energy polarization, assuming perfectly ordered magnetic field perpendicular to the line of sight (Zhang & Böttcher 2013)

• Synchrotron polarization:

Standard Rybicki & Lightman description

• SSC Polarization:

Bonometto & Saggion (1974) for Compton scattering in Thomson regime

• External-Compton emission (relativistic e⁻): Unpolarized:



The Doppler Factor Crisis



VHE γ-ray variability on time scales as short as a few minutes! γ–γ opacity constraints, assuming isotropic emission in the co-moving frame of the emission region

=> Γ ~ δ **>** 50

Strong disagreement with observed superluminal motions!



Edited by M. Boettcher, D. E. Harris, and H. Krawczynski WILEY-VCH

Relativistic Jets from Active Galactic Nuclei

