# Astrophysical Radiation Mechanisms and Polarization



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- 1. Introduction to Radiation Transfer
- 2. Blackbody Spectrum Brightness Temperature
- 3. Introduction to Synchrotron Radiation (spectra, energy losses, polarization, Stokes parameters)
- 4. Introduction to Compton Scattering (spectra, energy losses, Compton polarization, X-ray/γ-ray polarimetry)

#### Radiation Transfer









 $400$ 

TiO

600

Wavelength (nm)

700

1) Absorption spectra

Bright background source behind a cold absorber

#### Radiation Transfer (III)

Special Cases

 $I_{v}(\tau_{v}) = I_{v}(0) e^{-\tau_{v}} + S_{v} (1 - e^{-\tau_{v}})$ 

2) Emission spectra

No significant background source

 $(I_{\nu}(0) \approx 0)$ 

I) Optically thick emission:

 $(\tau_{v} >> 1)$ 



#### Radiation Transfer (IV)

Special Cases

 $I_{v}(\tau_{v}) \approx I_{v}(0) e^{-\tau_{v}} + S_{v} \text{ (1)} \approx g_{v}^{\tau_{v}} \text{/s}$ 

2) Emission spectra

No significant background source

 $(I_2(0) \approx 0)$ 

II) Optically thin emission:

 $(\tau_{\lambda} << 1)$ 





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### Thermal Blackbody Radiation

$$
I_{v}(\tau_{v}) = I_{v}(0) e^{-\tau_{v}} + S_{v} (1 - e^{-\tau_{v}})
$$



#### Thermal Blackbody Spectrum



#### Brightness Temperature

Define *Brightness Temperature* T<sub>b</sub> by setting measured intensity I<sub>v</sub> equal to Blackbody in Rayleigh-Jeans Limit:

$$
I_{v} = 2 (v^2/c^2) k_B T_b
$$

$$
\Rightarrow T_b = \frac{I_v c^2}{2 v^2 k_B}
$$

Note:  $T<sub>b</sub>$  usually has nothing to do with the source's real temperature!

# Brightness Temperature

Brightness temperatures  $T_b > 10^{12}$  K seem unphysical because of strong Compton scattering (see point 4 below)



# Relativistic Beaming / Boosting



### Relativistic Beaming / Boosting



(if the size of the emitter is determined from variability)



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### Cyclotron/Synchrotron Radiation



### Synchrotron Radiation

Relativistic electrons:

 $v_{\rm sv}$  (γ) ~ 4.2\*10<sup>6</sup> (B/G) γ<sup>2</sup> Hz

Power output into synchrotron radiation (single electron):

$$
\left(\frac{dE}{dt}\right)_{\text{sy}}\left(\gamma\right) = \frac{4}{3} \text{ c } \sigma_{\text{T}} \text{ u}_{\text{B}} \gamma^2 \beta^2
$$

![](_page_16_Figure_5.jpeg)

![](_page_17_Picture_0.jpeg)

Simple delta-function approximation for single-electron emissivity:

$$
P_v(\gamma) \approx \left(\frac{dE}{dt}\right)_{sy} \delta(v - v_{sy}[\gamma])
$$

$$
\nu_{\text{sy}}(\gamma) = \nu_0 \, \gamma^2
$$

 $j_v = \int_1^{\infty} d\gamma P_v(\gamma) N_e(\gamma) \sim N_e(\gamma_c) v^{1/2}$  $\gamma_c = (v/v_0)^{1/2}$ 

#### Synchrotron Radiation

Power-law distribution of relativistic electrons:

 $N_e(\gamma) \sim \gamma^{-p}$ 

If there are electrons with  $v = v_{sy}(\gamma)$ , then:

![](_page_18_Figure_4.jpeg)

![](_page_19_Picture_0.jpeg)

Preferred direction of E-field vectors of radiation

![](_page_19_Figure_2.jpeg)

 $E_{rad}$  predominantly  $\perp$  to projection of B

# Synchrotron Polarization

Calculate polarization-dependent intensities  $I_{\nu}^{\perp}$  and  $I_{\nu}^{\parallel}$ perpendicular and parallel to B-field projection

$$
\frac{\text{Degree of Polarization:}}{\prod_{max} I_{max} + I_{min}} = \frac{I_v^{\perp} - I_v^{\parallel}}{I_v^{\perp} + I_v^{\parallel}}
$$

In perfectly ordered, homogeneous B-field:

$$
\Pi = \frac{p+1}{p+7/3} = \frac{\alpha+1}{\alpha+5/3} \qquad (\alpha = \frac{p-1}{2})
$$

 $p = 2 \rightarrow \Pi = 69 \%$  $p = 3 \rightarrow \Pi = 75 \%$ 

# Stokes Parameters

![](_page_21_Figure_1.jpeg)

tan(2 $\chi$ )

#### Define Stokes Parameters:

I = Total intensity -> Polarized Intensity  $I_{pol} = \Pi I$  $Q = I_{pol} \cos(2\beta) \cos(2\chi)$  ( $\beta$  = phase-shift y vs. x => circ. pol.) U = I<sub>pol</sub> cos(2β) sin(2χ) V = I<sub>pol</sub> sin(2 $\beta$ ) = circularly polarized intensity (typically,  $\beta$  << 1)

![](_page_21_Picture_4.jpeg)

# Stokes Parameters

#### Stokes parameters are additive:

![](_page_22_Figure_2.jpeg)

Simply add up Stokes parameters from different zones:

 $I_{\text{total}} = \sum_{k=1}^{N} I_k$  $\prod_{i} \equiv \frac{\sqrt{Q_{total}}^2 + U_{total}^2 + V_{total}^2}{\sqrt{Q_{total}}^2 + Q_{total}^2}$  $I_{total}$  $Q_{total} = \sum_{k=1}^{N} Q_k$  $\tan(2\chi) = \frac{U_{total}}{Q}$  $U_{total} = \sum_{k=1}^{N} U_k$  $V_{\text{total}} = \sum_{k=1}^{N} V_k$ 

![](_page_23_Picture_0.jpeg)

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# Compton Scattering

![](_page_24_Figure_1.jpeg)

For  $\varepsilon'$  << 1  $\rightarrow \varepsilon'_{s} \approx \varepsilon'$  (elastic scattering – Thomson Regime) For  $\varepsilon' >> 1 \rightarrow \varepsilon'_{s} \sim 1$  (inelastic scattering – Klein-Nishina [KN] Regime)

$$
\sigma_C(\epsilon') = \frac{\pi r_e^2}{\epsilon'^2} \left( 4 + \frac{2\epsilon'^2 (1+\epsilon')}{(1+2\epsilon')^2} + \frac{\epsilon'^2 - 2\epsilon' - 2}{\epsilon'} \ln(1+2\epsilon') \right)
$$

#### Compton Scattering

![](_page_25_Figure_1.jpeg)

# Compton Scattering by Relativistic Electrons – Thomson Regime

![](_page_26_Figure_1.jpeg)

ph in electron rest frame ('):  $\varepsilon' = \varepsilon \gamma (1 - \beta \mu)$ In Thomson Regime  $(ε' < 1)$ :  $\epsilon_{\rm c}^{\prime} = \epsilon^{\prime}$ Doppler boost into lab frame:  $\varepsilon_{\rm s} = \gamma \varepsilon_{\rm s}' = \varepsilon \gamma^2 (1 - \beta \mu)$ 

Concentrated in forward direction  $(\Omega_e)$ 

Thomson approximation for differential cross section:  $\frac{d\sigma_{C}}{d\epsilon d\Omega_{s}} = \sigma_{T} \delta(\epsilon_{s} - \epsilon \gamma^{2} [1 - \beta \mu]) \delta(\Omega_{s} - \Omega_{e})$ 

# Compton Losses and Spectra

Power output into Compton radiation (single electron):

$$
\left(\frac{dE}{dt}\right)_C \left(\gamma\right) = \frac{4}{3} c \sigma_T u_{\text{rad}} \gamma^2 \beta^2
$$

Delta-function approximation for single-electron emissivity:

$$
P_v(\gamma) \approx \left(\frac{dE}{dt}\right)_C \delta(v - v_C[\gamma])
$$

$$
v_C(\gamma) \sim v_0 \gamma^2
$$

$$
j_v = \int_1^\infty d\gamma \, P_v(\gamma) \, N_e(\gamma) \sim N_e(\gamma_c) \, v^{1/2}
$$

$$
\gamma_c = (v/v_0)^{1/2}
$$

#### Compton Spectra

Power-law distribution of relativistic electrons:

 $N_e(\gamma) \sim \gamma^{-p}$ 

If there are electrons with  $v = v_C(y)$ , then:

![](_page_28_Figure_4.jpeg)

# Compton Scattering by Relativistic Electrons – KN Regime

ph in electron rest frame ('):  $\varepsilon' = \varepsilon \gamma (1 - \beta \mu)$ In the KN-Regime  $(\varepsilon' >> 1)$ :  $\varepsilon_{\rm s}^{\prime} = 1$ Doppler boost into lab frame:  $^{\prime}=\gamma$ 

 $\Rightarrow$  Photon takes all of the electron's energy  $(\varepsilon_{s} \sim \varepsilon \gamma^{2} > \gamma \rightarrow$  would violate energy conservation!)

![](_page_29_Figure_3.jpeg)

Cut-off in the resulting Comptonscattered spectra around  $\epsilon_{\rm s} \sim 1/\epsilon$ 

![](_page_30_Figure_0.jpeg)

#### Compton Polarization

#### Compton cross section is polarization-dependent:

$$
\frac{d\sigma}{d\Omega} = \frac{r_0^2}{4} \left(\frac{\epsilon'}{\epsilon}\right)^2 \left(\frac{\epsilon}{\epsilon'} + \frac{\epsilon'}{\epsilon} - 2 + 4\left[\vec{e'} \cdot \vec{e'}\right]^2\right)
$$

(e- rest frame)

 $\varepsilon = h \nu/(m_{\rm e} c^2)$ 

Thomson regime:  $\varepsilon \approx \varepsilon'$  $\Rightarrow$ dσ/dΩ = 0 if e⋅e' = 0

 $\Rightarrow$  Scattering preferentially in the plane perpendicular to  $\overrightarrow{e}$ !

Preferred EVPA is preserved.

Scattering of polarized rad. by relativistic  $e^- \implies \Pi$  reduced to  $\sim \frac{1}{2}$ of target-photon polarization.

![](_page_31_Figure_9.jpeg)

### X-ray Polarimeters

![](_page_32_Picture_1.jpeg)

#### INTEGRAL

![](_page_32_Picture_3.jpeg)

![](_page_32_Picture_4.jpeg)

![](_page_32_Picture_5.jpeg)

![](_page_32_Picture_7.jpeg)

# X-Ray Polarimeters

![](_page_33_Figure_1.jpeg)

![](_page_34_Figure_0.jpeg)

![](_page_34_Figure_1.jpeg)

(POLAR: Kole et al. 2016)

![](_page_34_Figure_3.jpeg)

#### Gamma-Ray Polarimetry with Fermi-LAT  $\int_{k}$

![](_page_35_Picture_1.jpeg)

 $\vec{e}$ 

![](_page_35_Picture_2.jpeg)

e<sup>+</sup>e<sup>-</sup> pair is preferentially produced in the plane of  $(\vec{k}, \vec{e})$  of the *γ*-ray. Potentially detectable at E < 200 MeV → PANGU / eASTROGAM

![](_page_36_Picture_0.jpeg)

![](_page_39_Picture_0.jpeg)

1. Introduction to Radiation Transfer

2. Radiation Mechanisms: Introduction to Synchrotron: Radiation (spectra, energy losses, polarization, Stokes parameters)

3. Introduction to Compton Scattering (spectra, energy losses, Compton polarization, X-ray/γ-ray polarimetry)

4. Introduction to  $\gamma\gamma$  absorption / pair production, Doppler factor estimate from γγ opacity

#### γγ **Absorption and Pair Production**

Threshold energy  $\varepsilon_{thr}$  of a *γ*-ray to interact with a background photon with energy  $\varepsilon_1$ : 2

![](_page_40_Figure_2.jpeg)

![](_page_41_Picture_0.jpeg)

#### Delta-Function Approximation:

$$
\sigma_{\gamma\gamma}^{\delta}(\epsilon_1,\epsilon_2)=\frac{1}{3}\,\sigma_T\,\epsilon_1\,\delta\left(\epsilon_1-\frac{2}{\epsilon_2}\right)
$$

VHE gamma-rays interact preferentially with IR photons:

$$
\lambda_2 = 2.4\,E_{1,\text{TeV}}\,\,\mu\text{m}
$$

# Spectrum of the Extrgalactic Background Light (EBL)

![](_page_42_Figure_1.jpeg)

#### EBL Absorption

![](_page_43_Figure_1.jpeg)

#### γγ Absorption Intrinsic to the Source

Optical depth to  $γγ$ -absorption:

$$
\tau_{\gamma\gamma}(\epsilon_{\gamma}) \sim n_{ph} \left(\frac{2}{\epsilon_{\gamma}}\right) R \sigma_{T}
$$

$$
n_{ph} \sim \frac{L}{4\pi R^2 c \, \varepsilon \, m_e c^2} = \frac{4\pi \, d_L^2 F}{4\pi R^2 c \, \varepsilon \, m_e c^2}
$$

Importance of intrinsic  $\gamma\gamma$ -absorption is estimated by the Compactness Parameter:

$$
\ell = \frac{L_{\gamma} \sigma_T}{4 \pi R \langle \epsilon \rangle m_e c^3}
$$

#### γγ Absorption Intrinsic to the Source

Estimate R from variability time scale:

 $R \sim c \Delta t_{var}$ 

**Optical depth to γγ-absorption:** 

![](_page_45_Figure_4.jpeg)

![](_page_45_Figure_5.jpeg)

With  $F_x$  and  $\Delta t_{var}$  from PKS 2155-304:  $\tau_{\gamma\gamma}$  (ε<sub>TeV</sub>) >> 1

# Relativistic Beaming / Boosting

![](_page_46_Figure_1.jpeg)

#### Relativistic Beaming / Boosting

![](_page_47_Figure_1.jpeg)

#### γγ Absorption Intrinsic to the Source

Optical depth to *yy*-absorption:

$$
\tau_{\gamma\gamma}(\epsilon_{\gamma}) \sim \frac{d_{L}^{2} F_{\epsilon}(\frac{2}{\epsilon_{\gamma}}) \sigma_{T}}{\Delta t_{var}(\frac{2}{\epsilon_{\gamma}}) m_{e} c^{4}}
$$

$$
F_{\varepsilon} = \delta^{-(3+\alpha)} F_{\varepsilon}^{obs}
$$

$$
\varepsilon_{\gamma} = \varepsilon_{\gamma}^{obs} / \delta
$$

$$
\Delta t_{var} = \delta \Delta t_{var}^{obs}
$$

$$
\boxed{\Rightarrow \tau_{\gamma\gamma} \propto \delta^{-(5+\alpha)}}
$$

![](_page_50_Figure_0.jpeg)

![](_page_51_Picture_0.jpeg)

![](_page_51_Picture_1.jpeg)

- Class of AGN consisting of BL Lac objects and gamma-ray bright quasars
- Rapidly (often intra-day) variable
- Strong gamma-ray sources
- Radio jets, often with superluminal motion
- Radio and optical polarization

# Blazar Spectral Energy Distributions (SEDs)

![](_page_52_Figure_1.jpeg)

Flux and Polarization **Variability** 

Multi-wavelength variability on various time scales (months – minutes) Sometimes correlated, sometimes not

Observed polarization fractions  $\Pi_{\rm obs}$  <~ 10 % <<  $\Pi_{\rm max}$ 

=> Not perfectly ordered magnetic fields!

Both degree of polarization and polarization angles vary. Swings in polarization angle sometimes associated with high-energy flares!

![](_page_53_Figure_5.jpeg)

# **Open Physics Questions**

- Source of Jet Power (Blandford-Znajek / Blandford/Payne?)
- Physics of jet launching / collimation / acceleration – role / topology of magnetic fields
- Composition of jets (e--p or e+-e- plasma?) leptonic or hadronic high-energy emission?
- Mode of particle acceleration (shocks / shear layers / magnetic reconnection?) - role of magnetic fields
- Location of the energy dissipation / gamma-ray emission region

# Blazar Models

![](_page_55_Figure_1.jpeg)

#### Blazar Models

Injection, acceleration of ultrarelativistic electrons and protons

 $\mathsf{Q}_{\mathsf{e},\mathsf{p}}$ 

ν Ļ. ν

( γ,t)

![](_page_56_Figure_2.jpeg)

Proton-

induced

#### Requirements for lepto-hadronic models

- To exceed p-γ pion production threshold on interactions with synchrotron (optical) photons:  $\mathsf{E}_\mathsf{p}$  > 7x10<sup>16</sup> E<sup>-1</sup><sub>ph,eV</sub> eV
- For proton synchrotron emission at multi-GeV energies:  $E_p$  up to  $\sim 10^{19}$  eV (=> UHECR)
- Require Larmor radius

 $r_1 \sim 3x10^{16}$  E<sub>19</sub>/B<sub>G</sub> cm ≤ a few x 10<sup>15</sup> cm => B ≥ 10 G (Also: to suppress leptonic SSC component below synchrotron) – inconsistent with radio-core-shift measurements if emission region is located at  $\sim$  pc scales (e.g., Zdziarski & Böttcher 2015).

• Low radiative efficiency: Requiring jet powers  $L_{\text{jet}} \sim L_{\text{Edd}}$ 

#### SED Model Fit Degeneracy

RGB J0710+591 (HBL)

![](_page_58_Figure_2.jpeg)

#### Polarization Induced by Anisotropic Compton Scattering

![](_page_59_Figure_1.jpeg)

• Thermal + Non-Thermal Electron Distributions from Diffusive Shock Acceleration

#### AO 0235+164

![](_page_60_Figure_1.jpeg)

(Baring et al. 2016)

#### Expected Polarization from Bulk Compton

![](_page_61_Figure_1.jpeg)

#### Polarization Induced by Anisotropic Scattering

![](_page_62_Figure_1.jpeg)

![](_page_62_Figure_2.jpeg)

#### Calculation of X-Ray and Gamma-Ray Polarization in Leptonic and Hadronic Blazar Models

Upper limits on high-energy polarization, assuming perfectly ordered magnetic field perpendicular to the line of sight (Zhang & Böttcher 2013)

Synchrotron polarization:

Standard Rybicki & Lightman description

**SSC Polarization:** 

Bonometto & Saggion (1974) for Compton scattering in Thomson regime

• External-Compton emission (relativistic e- ): **Unpolarized:**

![](_page_63_Figure_7.jpeg)

#### The Doppler Factor Crisis

![](_page_64_Figure_1.jpeg)

VHE  $γ$ -ray variability on time scales as short as a few minutes!

γ−γ opacity constraints, assuming isotropic emission in the co-moving frame of the emission region

 $\Rightarrow$   $\Gamma \sim \delta$  > 50

Strong disagreement with observed superluminal motions!

![](_page_65_Picture_0.jpeg)

Edited by M. Boettcher, D. E. Harris, and H. Krawczynski

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#### Relativistic Jets from **Active Galactic Nuclei**

![](_page_65_Picture_4.jpeg)